

WHAT IS CLAIMED IS:

1. A method of numerical analysis of a simulation of a physical system, the physical system being describable by field equations in which a parameter is identifiable as a one-form and solving for a field equation corresponding to the parameter results in a singular differential operation, the method comprising:

directly solving the field equations modified by addition of a dummy field by numerical analysis, and

outputting at least one parameter relating to a physical property of the system.

2. An apparatus for numerical analysis of a simulation of a physical system, the physical system being describable by field equations in which a parameter is identifiable as a one-form and solving for a field equation corresponding to the parameter results in a singular differential operation, the apparatus comprising:

means for solving by numerical analysis a modification of the field equations, the modification being an addition of a dummy field, and

means for outputting at least one parameter relating to a physical property of the system.

3. A data structure for use in numerical analysis of a simulation of a physical system, the physical system being describable by field equations in which a parameter is identifiable as a one-form and solving for a field equation corresponding to the parameter results in a singular differential operation, the field equations being modified by addition of a dummy field, wherein the data structure comprises the simulation of the physical system as a representation of an n -dimensional mesh in a predetermined domain of the physical system, the mesh comprising nodes and $n-1$ planes connecting these nodes thereby dividing said domain in n -dimensional first elements whereby each element is defined by 2^n node, the data structure being stored in a memory and comprising representations of the nodes and links between nodes, the data structure also including definitions of a parameter of the dummy field associated with the nodes of the mesh.

4. A data structure for use in numerical analysis of a simulation of a physical system, the physical system being describable by Maxwell's field equations of which the following is a representation:

$$\nabla \times \left(\frac{1}{\mu} \nabla \times \mathbf{A} \right) = \mathbf{J} - \varepsilon \frac{\partial}{\partial t} \left(\nabla V + \frac{\partial \mathbf{A}}{\partial t} \right)$$

$$\nabla \cdot \mathbf{A} = 0$$

$$-\nabla(\varepsilon \nabla V) = \rho$$

$$\mathbf{E} = -\nabla V - \frac{\partial \mathbf{A}}{\partial t}$$

$$\mathbf{B} = \nabla \times \mathbf{A}$$

where

$$\mathbf{J} = \mathbf{J}(\mathbf{E}, \mathbf{B}, t)$$

$$\rho = \rho(\mathbf{E}, \mathbf{B}, t)$$

the field equations being modified by addition of a dummy field, wherein the data structure comprises the simulation of the physical system as a representation of an n-dimensional mesh in a predetermined domain of the physical system, the mesh comprising nodes and links connecting these nodes thereby dividing said domain in n-dimensional first elements whereby each element is defined by 2^n nodes the data structure being stored in a memory and comprising nodes and links between nodes, the data structure also including definitions of a parameter of the dummy field associated with the nodes of the mesh.

5. A data structure for use in numerical analysis of a simulation of a physical system, the physical system being describable by Maxwell's field equations of which the following is a representation:

$$\nabla \times \left(\frac{1}{\mu} \nabla \times \mathbf{A} \right) = \mathbf{J} - \varepsilon \frac{\partial}{\partial t} \left(\nabla V + \frac{\partial \mathbf{A}}{\partial t} \right)$$

$$\nabla \cdot \mathbf{A} = 0$$

$$-\nabla(\varepsilon \nabla V) = \rho$$

$$\mathbf{E} = -\nabla V - \frac{\partial \mathbf{A}}{\partial t}$$

$$\mathbf{B} = \nabla \times \mathbf{A}$$

where

$$\mathbf{J} = \mathbf{J}(\mathbf{E}, \mathbf{B}, t)$$

$$\rho = \rho(E, B, t)$$

the field equations being modified by addition of a dummy field, wherein the data structure comprises the simulation of the physical system as a representation of an n-dimensional mesh in a predetermined domain of the physical system, the mesh comprising nodes and links connecting these nodes thereby dividing said domain in n-dimensional first elements whereby each element is defined by 2^n node the data structure being stored in a memory and comprising nodes and links between nodes, the data structure also including definitions of the vector potential A associated with the links of the mesh.

6. A program storage device readable by a machine and encoding a program of instructions for executing a method of numerically analyzing a simulation of a physical system, the physical system being describable by field equations in which a parameter is identifiable as a one-form and solving for a field equation corresponding to the parameter results in a singular differential operation, the method comprising:

directly solving the field equations modified by addition of a dummy field by numerical analysis, and

outputting at least one parameter relating to a physical property of the system.

7. A program storage device readable by a machine and encoding a program of instructions for executing a method of numerically analyzing a simulation of a physical system, the physical system being describable by Maxwell's field equations of which the following is a representation:

$$\nabla \times \left(\frac{1}{\mu} \nabla \times A \right) = J - \varepsilon \frac{\partial}{\partial t} \left(\nabla V + \frac{\partial A}{\partial t} \right)$$

$$\nabla \cdot A = 0$$

$$-\nabla(\varepsilon \nabla V) = \rho$$

$$E = -\nabla V - \frac{\partial A}{\partial t}$$

$$B = \nabla \times A$$

where

$$J = J(E, B, t)$$

$$\rho = \rho(E, B, t)$$

the method comprising:

directly solving the field equations modified by addition of a dummy field by numerical analysis, and

outputting at least one parameter relating to a physical property of the system.

8. A computer program product for numerical analysis of a simulation of a physical system, the physical system being describable by field equations in which a parameter is identifiable as a one-form and solving for a field equation corresponding to the parameter results in a singular differential operation, the computer program product comprising:

code for solving the field equations modified by addition of a dummy field by numerical analysis, and

code for outputting at least one parameter relating to a physical property of the system.

9. A computer program product for numerical analysis of a simulation of a physical system, the physical system being describable by Maxwell's field equations of which the following is a representation:

$$\nabla \times \left(\frac{1}{\mu} \nabla \times A \right) = J - \varepsilon \frac{\partial}{\partial t} \left(\nabla V + \frac{\partial A}{\partial t} \right)$$

$$\nabla \cdot A = 0$$

$$-\nabla(\varepsilon \nabla V) = \rho$$

$$E = -\nabla V - \frac{\partial A}{\partial t}$$

$$B = \nabla \times A$$

where

$$J = J(E, B, t)$$

$$\rho = \rho(E, B, t)$$

the computer program product comprising:

code for solving the field equations modified by addition of a dummy field by numerical analysis, and

code for outputting at least one parameter relating to a physical property of the system.

10. A method of numerical analysis of a simulation of a physical system, comprising: transmitting from a near location a description of the physical system to a remote location where a processing engine carries out a method of numerically analyzing a simulation of a physical system, the physical system being describable by field equations in which a parameter is identifiable as a one-form and solving for a field equation corresponding to the parameter results in a singular differential operation, the method comprising:

receiving at a near location at least one physical parameter related to the physical system;

directly solving the field equations modified by addition of a dummy field by numerical analysis; and

outputting at least one parameter relating to a physical property of the system.

11. An apparatus for numerical analysis of a simulation of a physical system, the physical system being describable by field equations in which a parameter is identifiable as a one-form and solving for a field equation corresponding to the parameter results in a singular differential operation, the apparatus comprising:

a solving component for solving by numerical analysis a modification of the field equations, the modification being an addition of a dummy field; and

an outputting component for outputting at least one parameter relating to a physical property of the system.

12. An apparatus for numerical analysis of a simulation of a physical system, the physical system being describable by Maxwell's field equations of which the following is a representation:

$$\nabla \times \left(\frac{1}{\mu} \nabla \times \mathbf{A} \right) = \mathbf{J} - \epsilon \frac{\partial}{\partial t} \left(\nabla V + \frac{\partial \mathbf{A}}{\partial t} \right)$$

$$\nabla \cdot \mathbf{A} = 0$$

$$-\nabla(\epsilon \nabla V) = \rho$$

$$\mathbf{E} = -\nabla V - \frac{\partial \mathbf{A}}{\partial t}$$

$$\mathbf{B} = \nabla \times \mathbf{A}$$

where

$$\mathbf{J} = \mathbf{J}(\mathbf{E}, \mathbf{B}, t)$$

$$\rho = \rho(\mathbf{E}, \mathbf{B}, t)$$

the apparatus comprising:

a solving component for directly solving the field equations modified by addition of a dummy field by numerical analysis; and

an outputting component for outputting at least one parameter relating to a physical property of the system.

13. A apparatus according to claim 12, wherein the modified field equations are given by:

$$\nabla \times \left(\frac{1}{\mu} \nabla \times \mathbf{A} \right) - \gamma \nabla \chi = \mathbf{J} - \epsilon \frac{\partial}{\partial t} \left(\nabla V + \frac{\partial \mathbf{A}}{\partial t} + \frac{\partial \nabla \chi}{\partial t} \right)$$

$$\nabla \cdot \mathbf{A} + \nabla^2 \chi = 0$$

$$-\nabla(\epsilon \nabla V) = \rho$$

$$\mathbf{E} = -\nabla \left(V + \frac{\partial \chi}{\partial t} \right) - \frac{\partial \mathbf{A}}{\partial t}$$

$$\mathbf{B} = \nabla \times (\mathbf{A} + \nabla \chi) \text{ where } \chi \text{ represents the dummy field and } \gamma \text{ is non-zero.}$$

14. An apparatus according to claim 13, wherein the representation of the physical system is a representation of an n-dimensional mesh in a predetermined domain of the physical system, the mesh comprising nodes and n-1 planes connecting these nodes thereby dividing said domain in n-dimensional first elements whereby each element is defined by 2^n nodes, a representation of the mesh being stored in a memory of a computer system as a data structure comprising nodes and links between nodes, the data structure also including definitions of the vector potential \mathbf{A} associated with the links of the mesh.

15. An apparatus according to claim 13, wherein the representation of the physical system is a representation of an n-dimensional mesh in a predetermined domain of the

physical system, the mesh comprising nodes and links connecting these nodes thereby dividing said domain in n-dimensional first elements whereby each element is defined by 2^n nodes, a representation of the mesh being stored in a memory of a computer system as a data structure comprising nodes and links between nodes, the data structure also including definitions of the dummy field χ associated with the nodes.

16. An apparatus according to claim 12 further comprising:

a creating component for creating a first additional node inside at least one of said first elements by completely splitting said first element into exactly 2^n n-dimensional second elements in such a manner that said first additional node forms a corner node of each of said second elements which results in the replacement of said first element by said 2^n n-dimensional second elements, wherein the creation component creates a second additional node inside at least one of said second elements by completely splitting said second element in exactly 2^n n-dimensional third elements in such a manner that said second additional node forms a corner node of each of said third elements which results in the replacement of said second element by said 2^n n-dimensional third elements, and

a storing component for storing representations of the first and second additional nodes in the memory of the computer system.